Machine Learning & Deep Learning (Barcha uchun)

<09> Softmax

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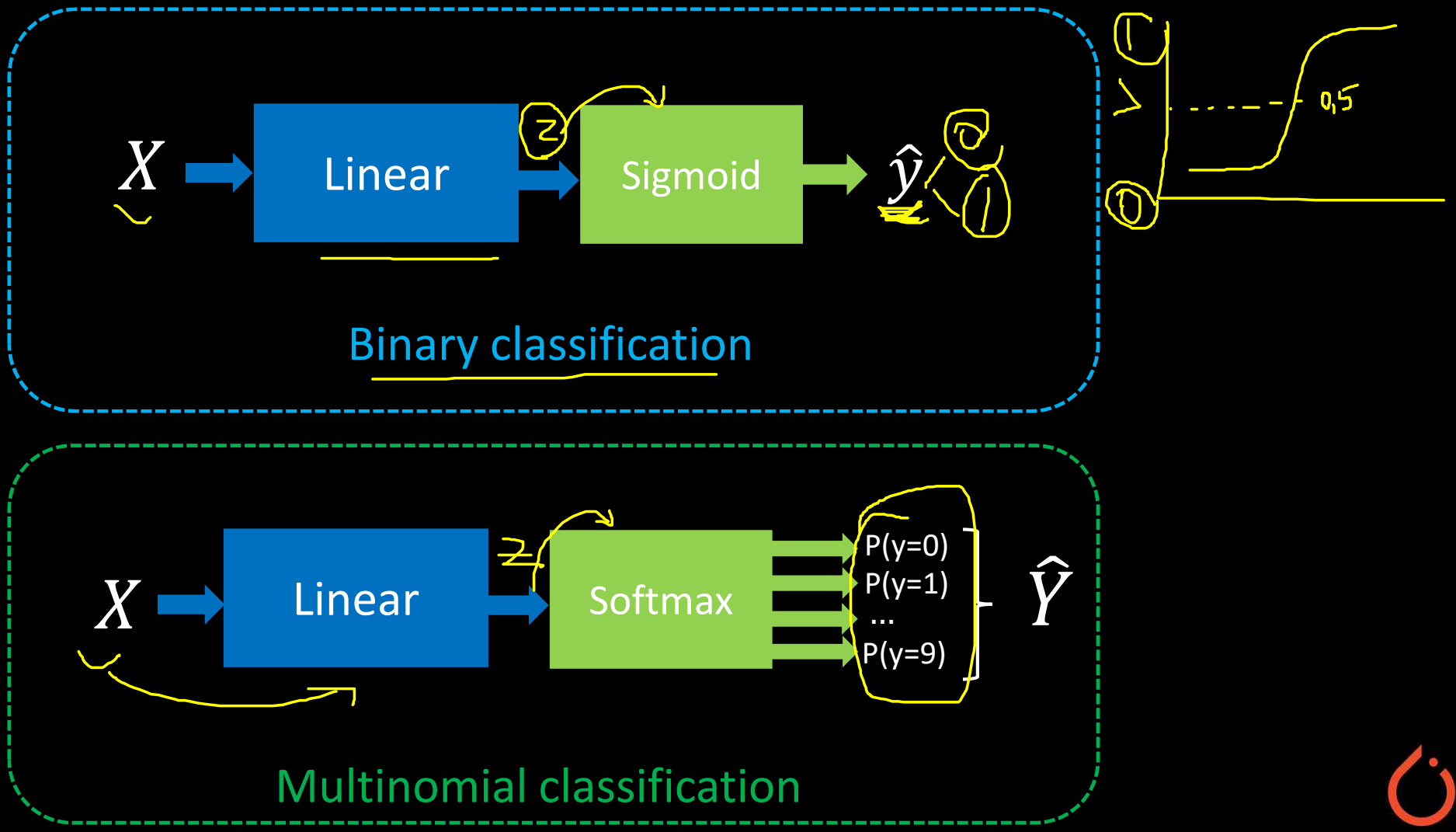
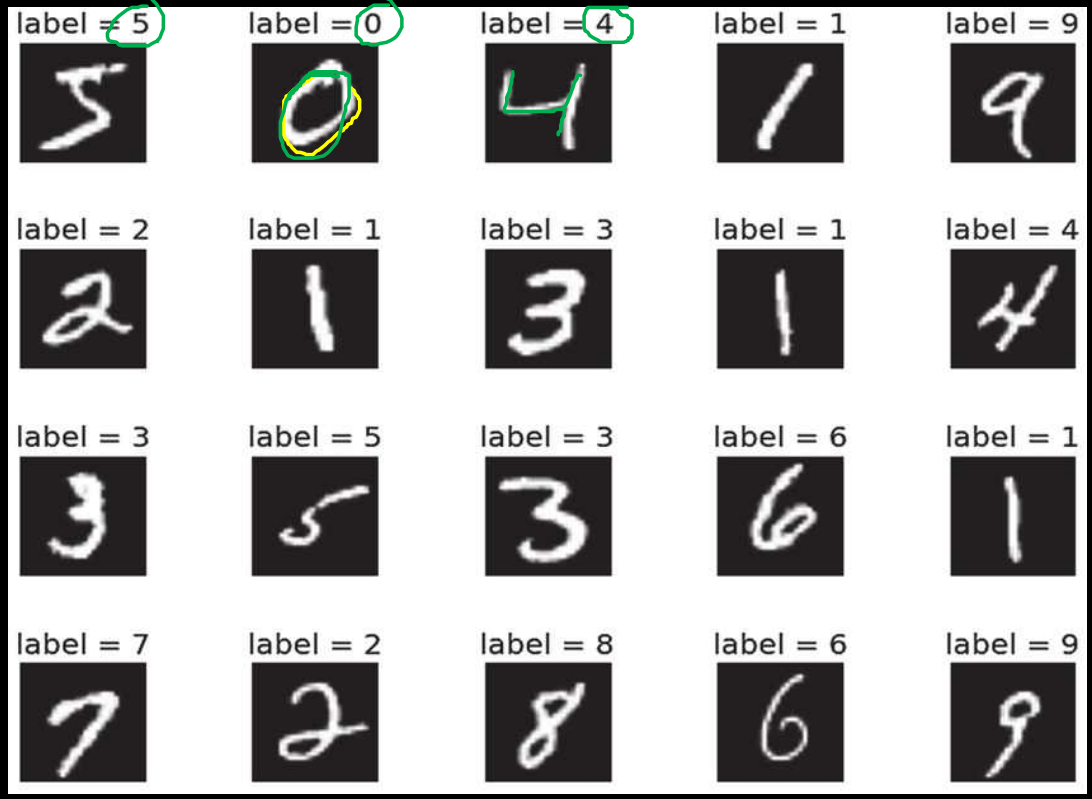
Ko’p sonli chiqish (output)



MNIST dataset : 10 labels

0 — 9



Softmax

$$\sigma(z)_j = \frac{e^{z_j}}{\sum_{k=1}^{K} e^{z_k}}$$

$j = 1, \ldots, K$ *uchun*

X ...

Linear

Z

2.0

1.0

0.1

Logits (Scores)

Softmax

0.7

0.2

0.1

P(y=0)

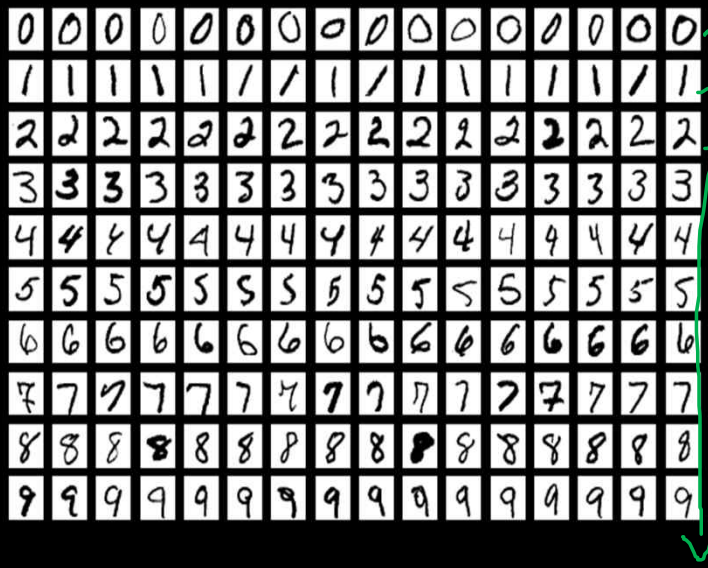
P(y=1)

P(y=2)

Probability

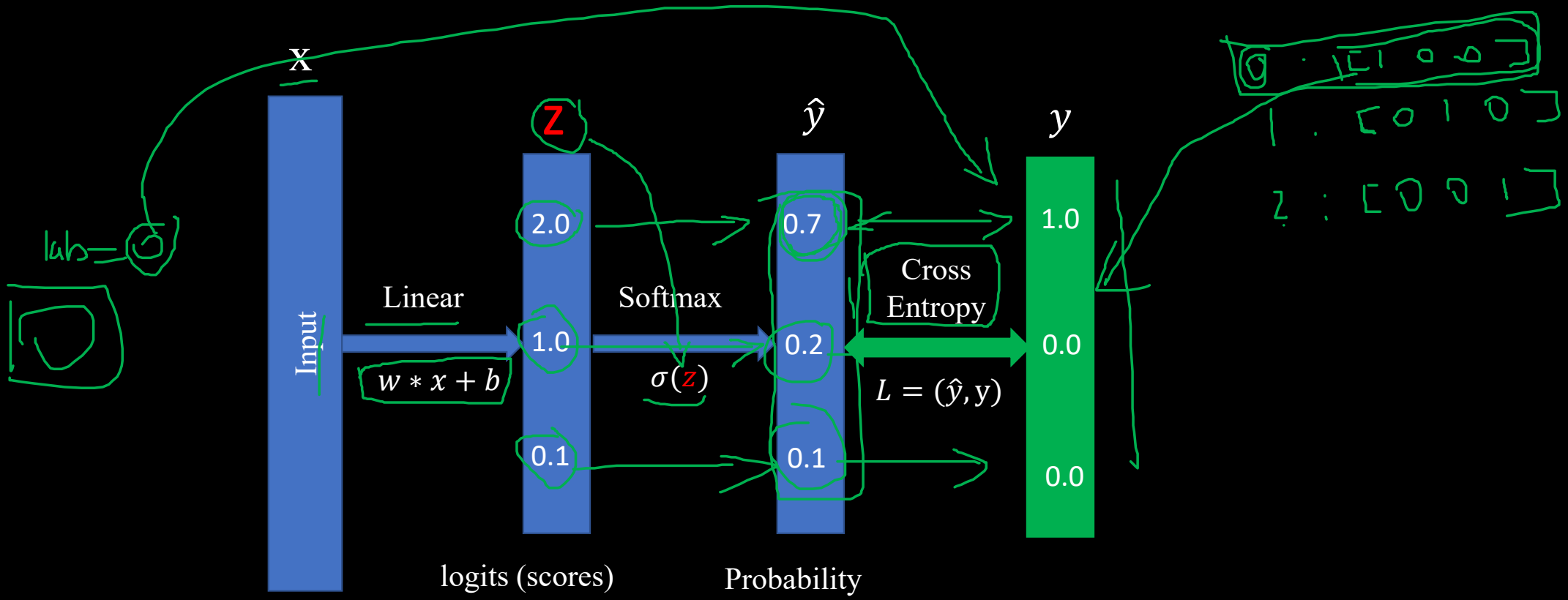
$\hat{Y}$

One-hot encoding (vector)

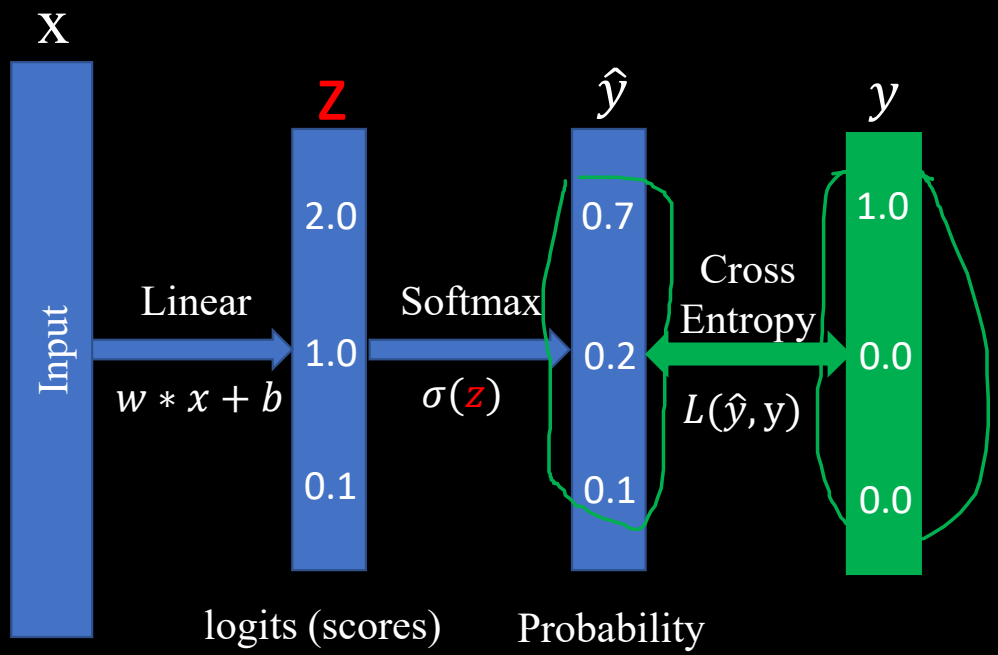


0	[1.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0]
1	[0.0 1.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0]
2	[0.0 0.0 1.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0]
3	[0.0 0.0 0.0 1.0 0.0 0.0 0.0 0.0 0.0 0.0]
4	[0.0 0.0 0.0 0.0 1.0 0.0 0.0 0.0 0.0 0.0]
5	[0.0 0.0 0.0 0.0 0.0 1.0 0.0 0.0 0.0 0.0]
6	[0.0 0.0 0.0 0.0 0.0 0.0 1.0 0.0 0.0 0.0]
7	[0.0 0.0 0.0 0.0 0.0 0.0 0.0 1.0 0.0 0.0]
8	[0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 1.0 0.0]
9	[0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 1.0]

Forward pass



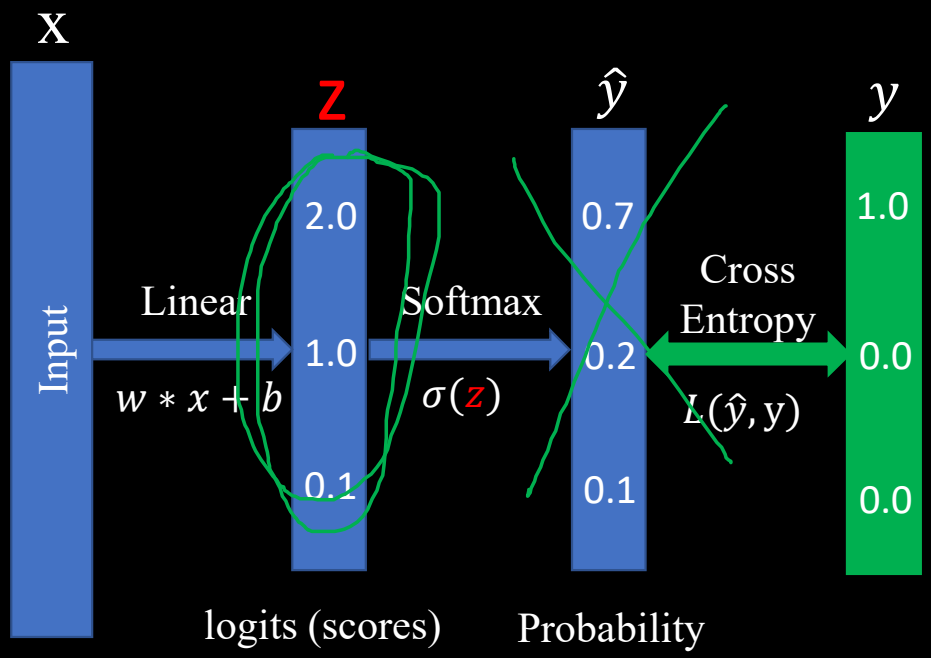
Loss: Cross Entropy




```python
import numpy as np
#one hot
# 0: 1 0 0
# 1: 0 1 0
# 2: 0 0 1

Y = np.array([1, 0, 0])  # haqiqiy qiymat

Y_pred1 = np.array([0.7, 0.2, 0.1]) # birinchi bashorat
Y_pred2 = np.array([0.1, 0.3, 0.6]) # ikkinchi bashorat

print("loss1= ", np.sum(-Y*np.log(Y_pred1))) # 0.35
print("loss2= ", np.sum(-Y*np.log(Y_pred2))) # 2.30
```

$$L(\hat{y}, y) = -y \log \hat{y}$$

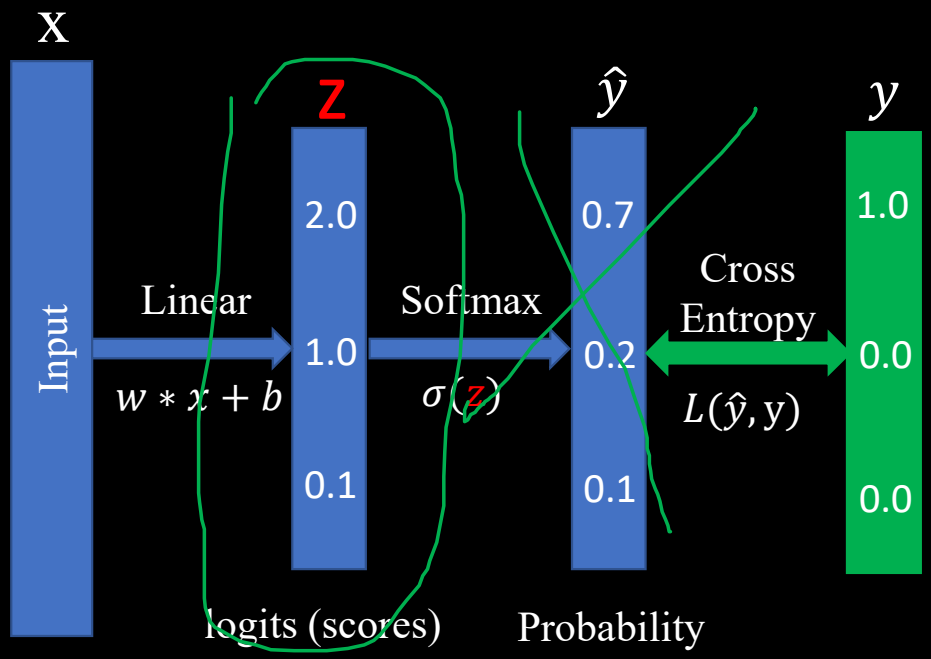
Cross Entropy: PyTorch




```python
# CrossEntropy
loss = nn.CrossEntropyLoss()

# Haqiqiy qiymat klass ko'rinishida one-hot enc emas
Y = tensor([0], requires_grad=False)

# Y_pred1 va Y_pred2 qiymatlari "logits", probability emas
Y_pred1 = tensor([[2.0, 1.0, 0.1]])
Y_pred2 = tensor([[0.5, 2.0, 0.3]])

l1 = loss(Y_pred1, Y)
l2 = loss(Y_pred2, Y)

print(f'PyTorch Loss1: {l1.item():.4f}') #0.41
print(f'PyTorch Loss2: {l2.item():.4f}') #1.84
```

$$L(\hat{y}, y) = -y \log \hat{y}$$

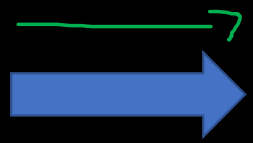
Cross Entropy: PyTorch (batch)

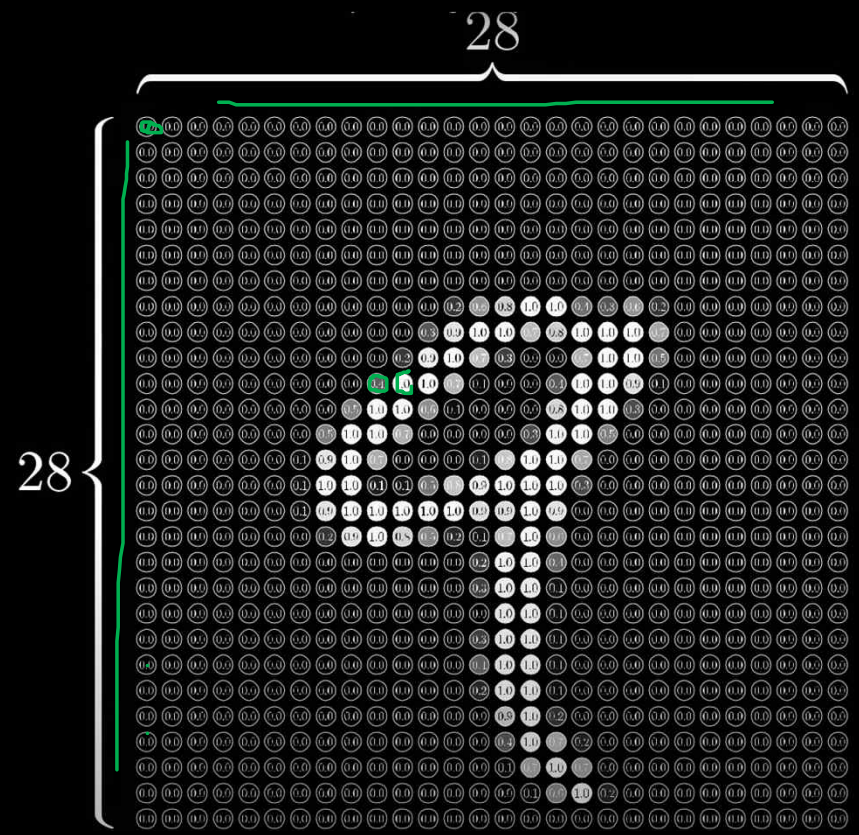



```python
# CrossEntropy
loss = nn.CrossEntropyLoss()

# Haqiqiy qiymat klass ko'rinishida (bu yerda batch)
Y = tensor([2, 0, 1], requires_grad=False)

#Y_pred1 va Y_pred2 qiymatlari "logits", probability emas
Y_pred1 = tensor([[0.1, 0.2, 0.9],
                  [1.1, 0.1, 0.2],
                  [0.2, 2.1, 0.1]]) # batch uchun

Y_pred2 = tensor([[0.8, 0.2, 0.3],
                  [0.2, 0.3, 0.5],
                  [0.2, 0.2, 0.5]])  # batch uchun

l1 = loss(Y_pred1, Y)
l2 = loss(Y_pred2, Y)

print(f'Batch Loss1:  {l1.data:.4f}')
print(f'Batch Loss2:  {l2.data:.4f}')
```

$$L(\hat{y}, y) = -y \log \hat{y}$$

MNIST

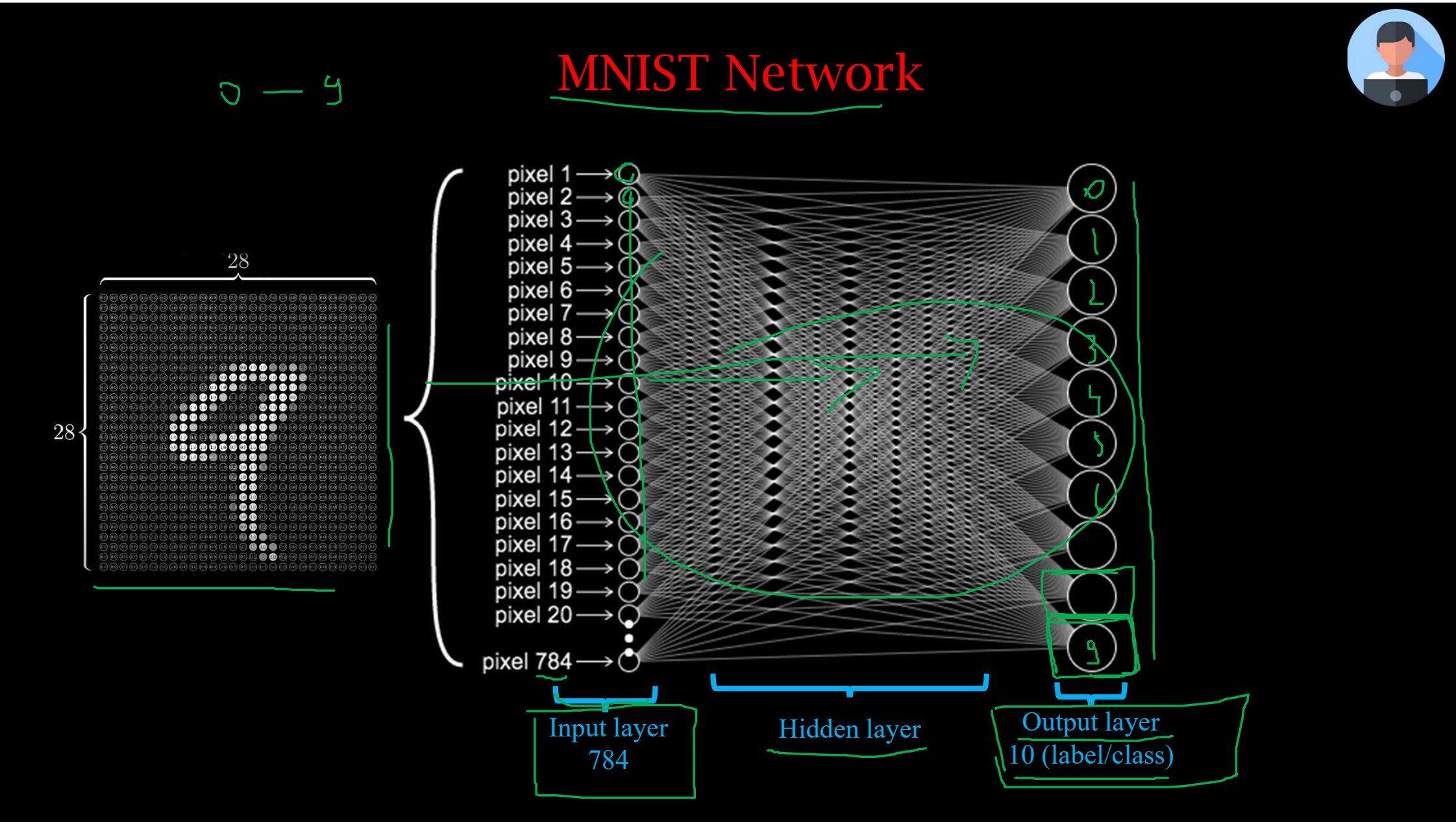




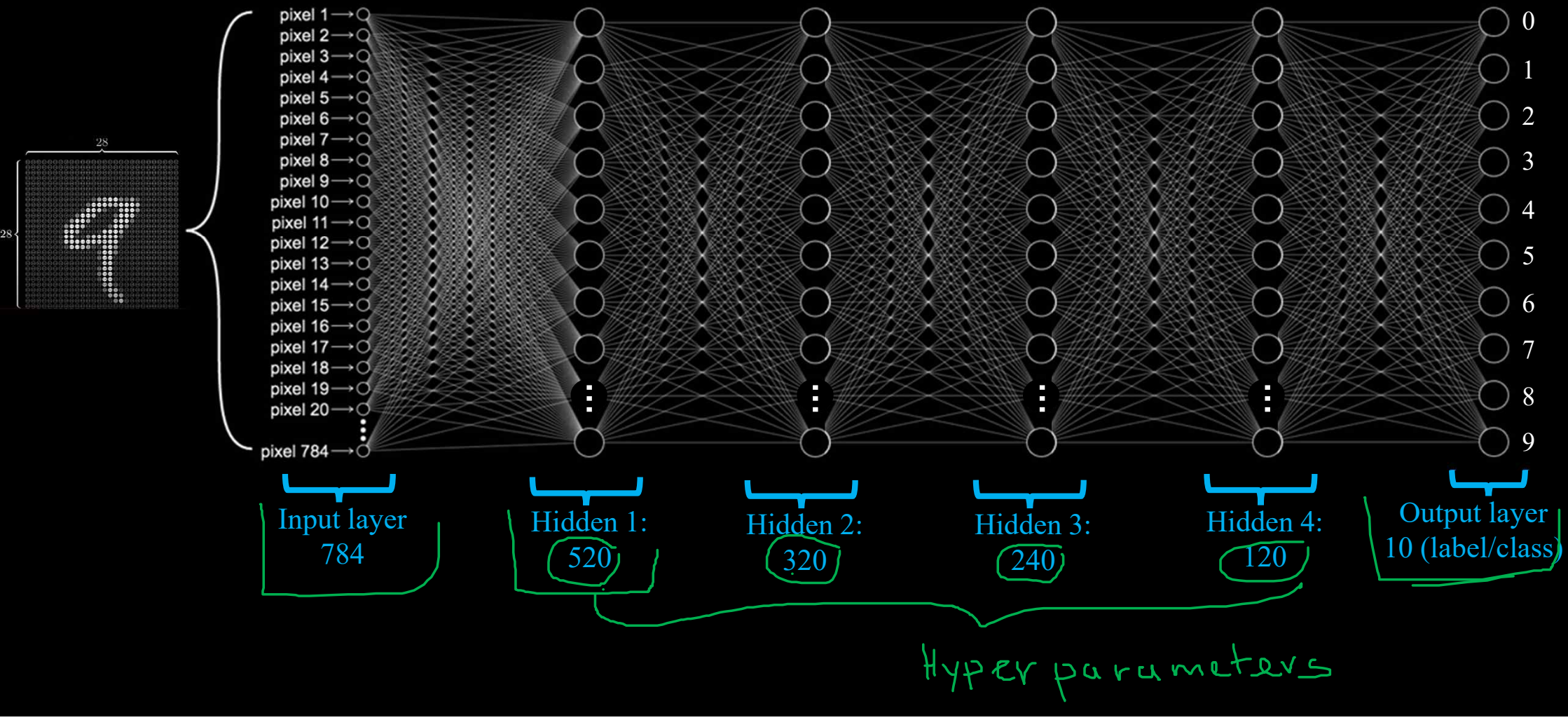
$1 \times 28 \times 28 = 784$

$3 \times 28 \times 28 = 784 \times 3$

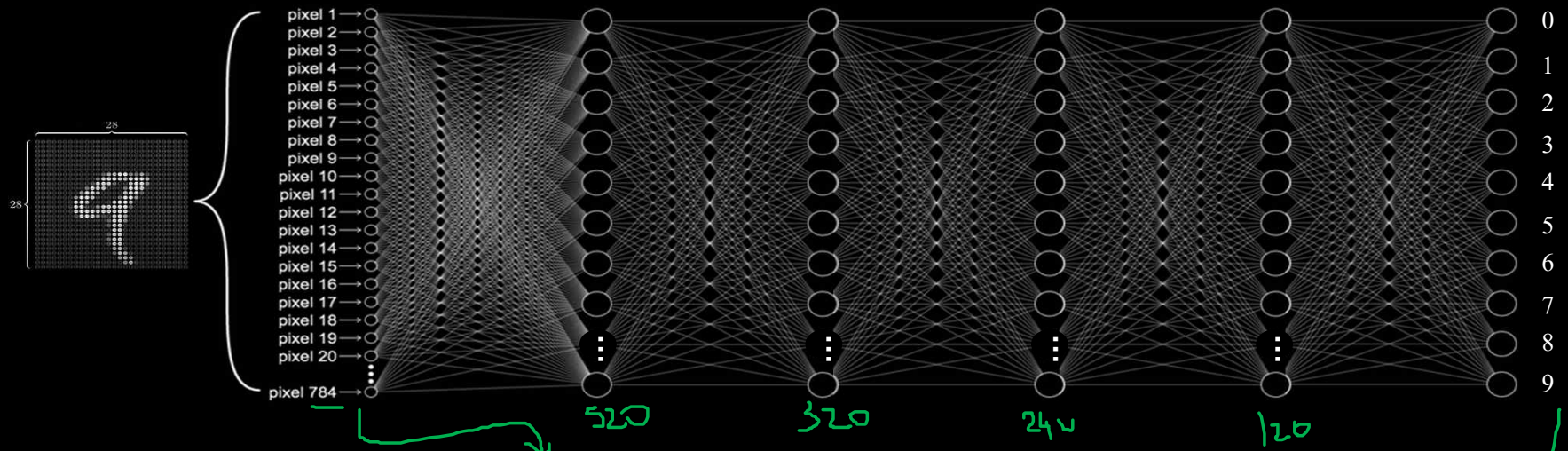
r g b


0 — 9
MNIST Network
28
28
pixel 1
pixel 2
pixel 3
pixel 4
pixel 5
pixel 6
pixel 7
pixel 8
pixel 9
pixel 10
pixel 11
pixel 12
pixel 13
pixel 14
pixel 15
pixel 16
pixel 17
pixel 18
pixel 19
pixel 20
pixel 784
0
1
2
3
4
5
9
Input layer
784
Hidden layer
Output layer
10 (label/class)

MNIST Network



MNIST Network




```
self.l1 = nn.Linear(784, 520)
self.l2 = nn.Linear(520, 320)
self.l3 = nn.Linear(320, 240)
self.l4 = nn.Linear(240, 120)
self.l5 = nn.Linear(120, 10)
```

MNIST